



Splitting Algebraic Loops for Improved Performance and Parallelization

Linköping, 03/02/2014

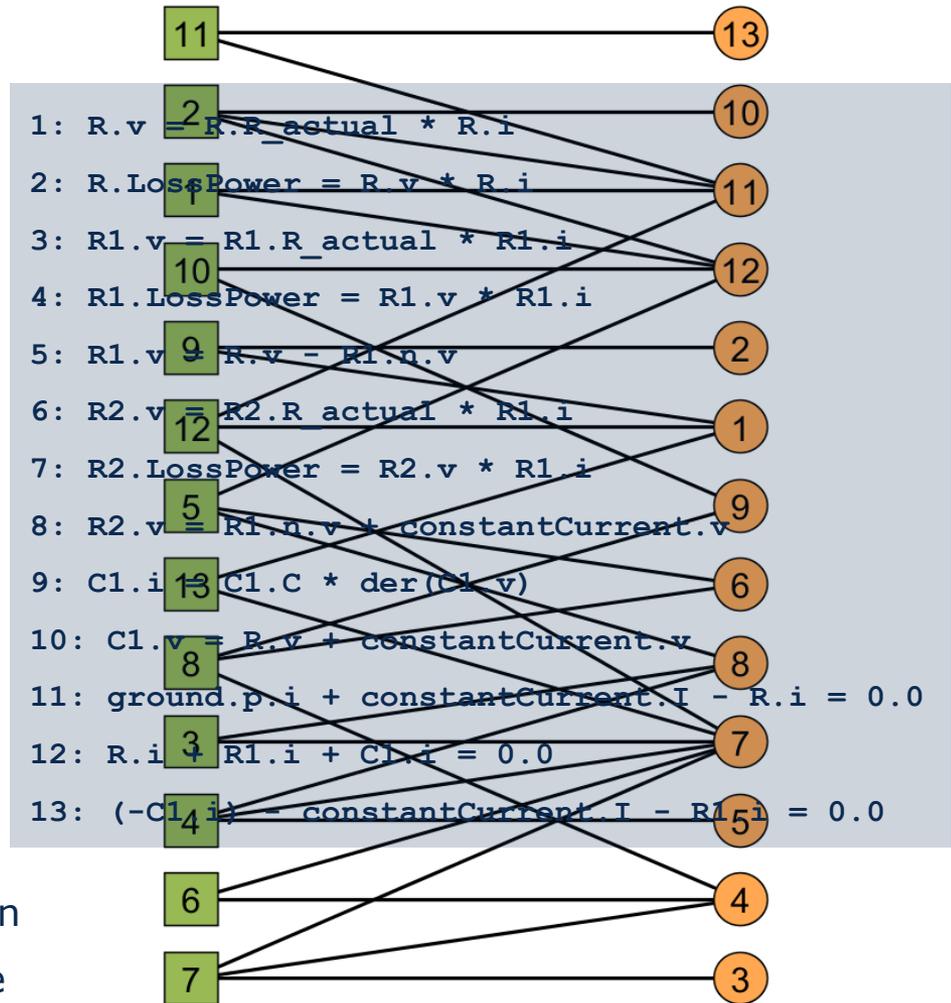
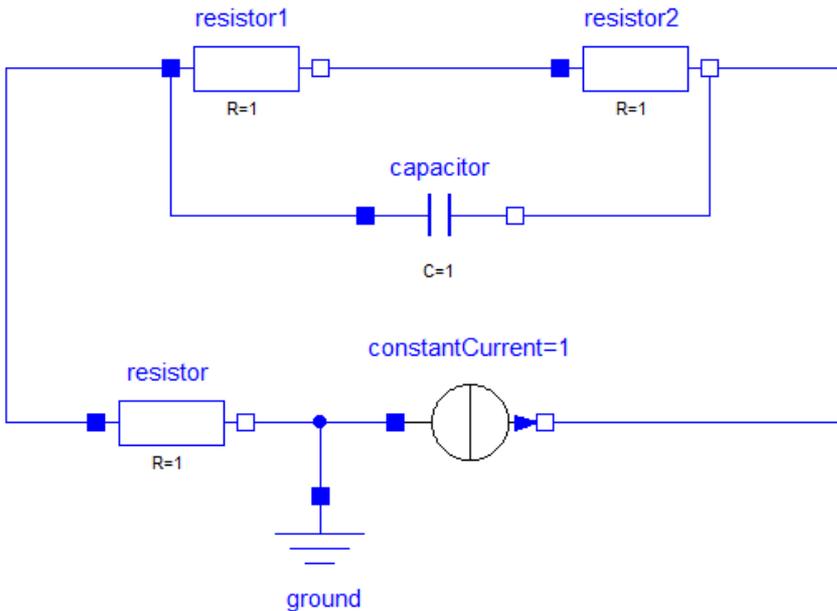


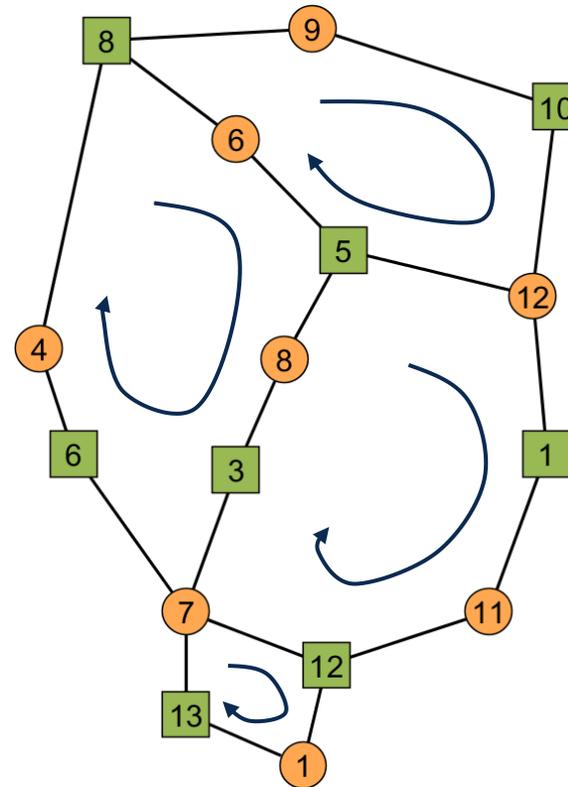
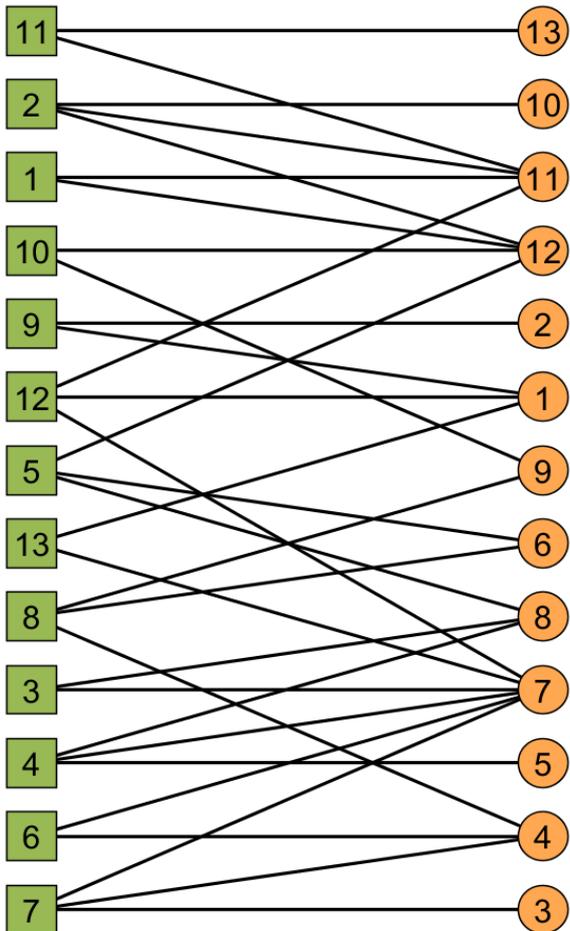
Outline

1. Algebraic Loop
2. Resolving Loops
3. Effects of Resolving Loops
4. Summary and Outlook



Algebraic Loops

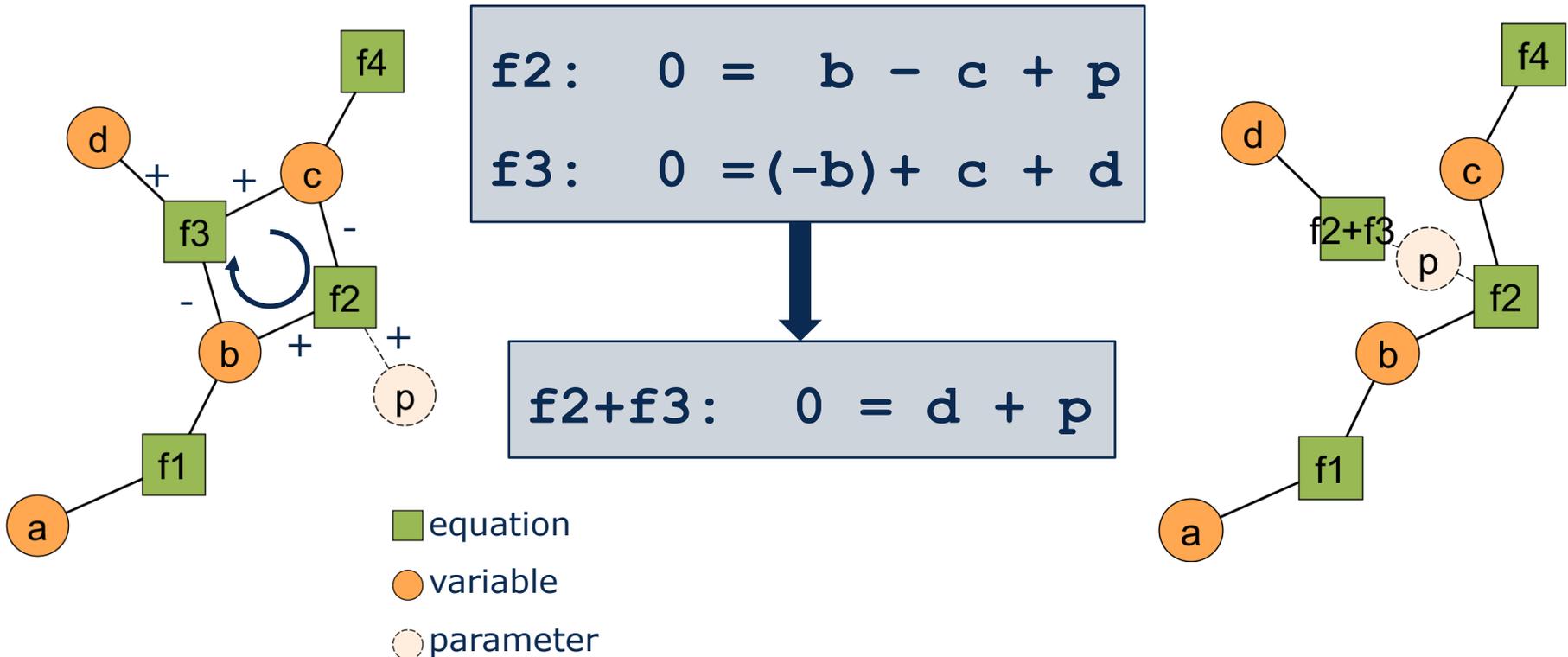




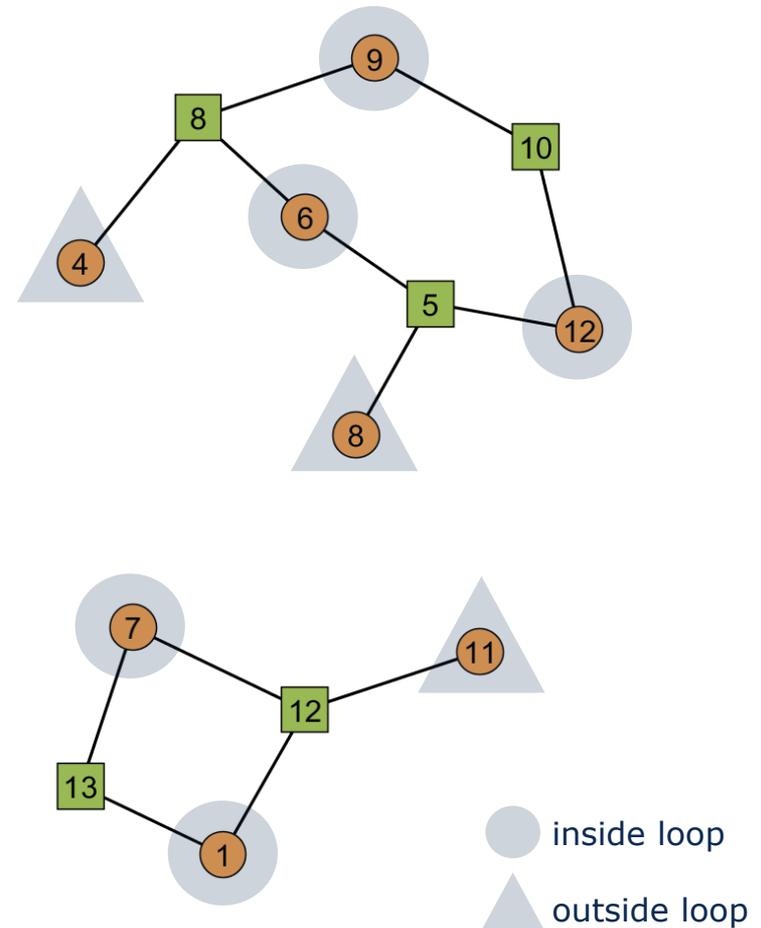
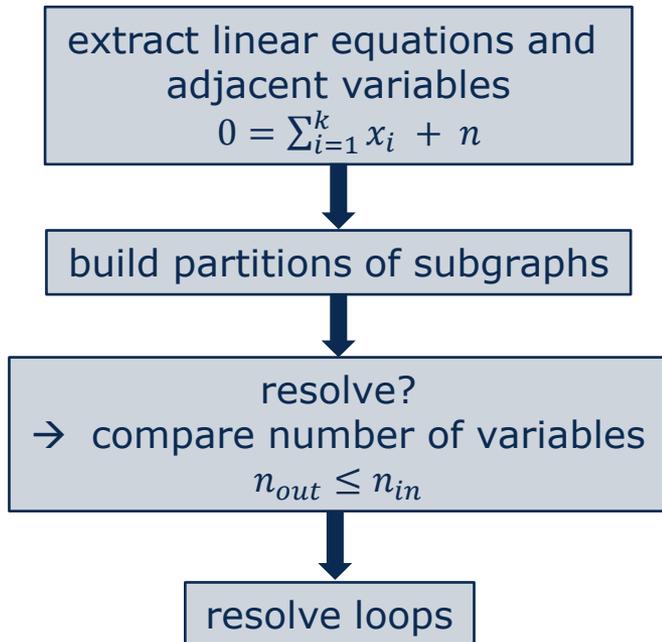
How to handle an algebraic loop?

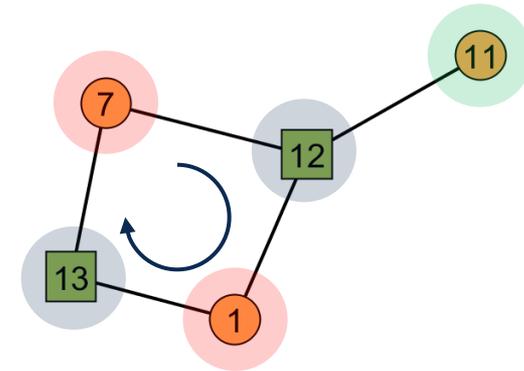
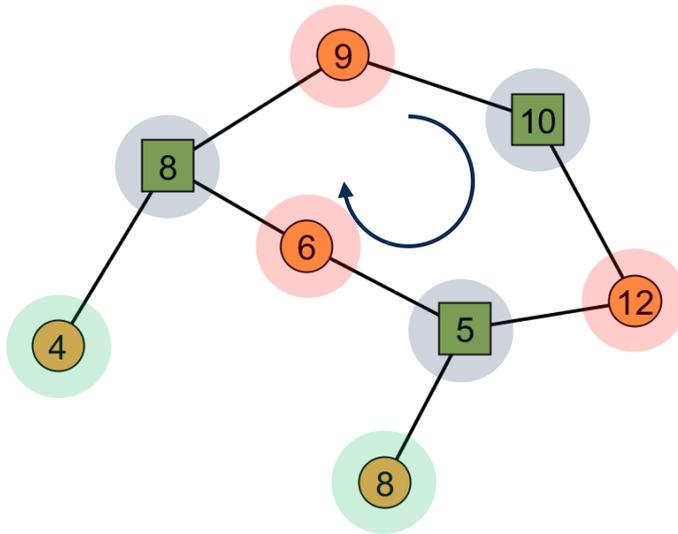
- Solving as an equation system with a linear or nonlinear solver routine
 - expensive solving of big equation systems
 - singular systems not treatable
 - special treatment to parallelize systems
- Choose tearing-variables + Newton iteration
 - tearing heuristic
 - reduce sparse system to dense system
- Splitting loop
 - resolve equations of the loop

What does it mean to resolve a loop?



Resolving Loops



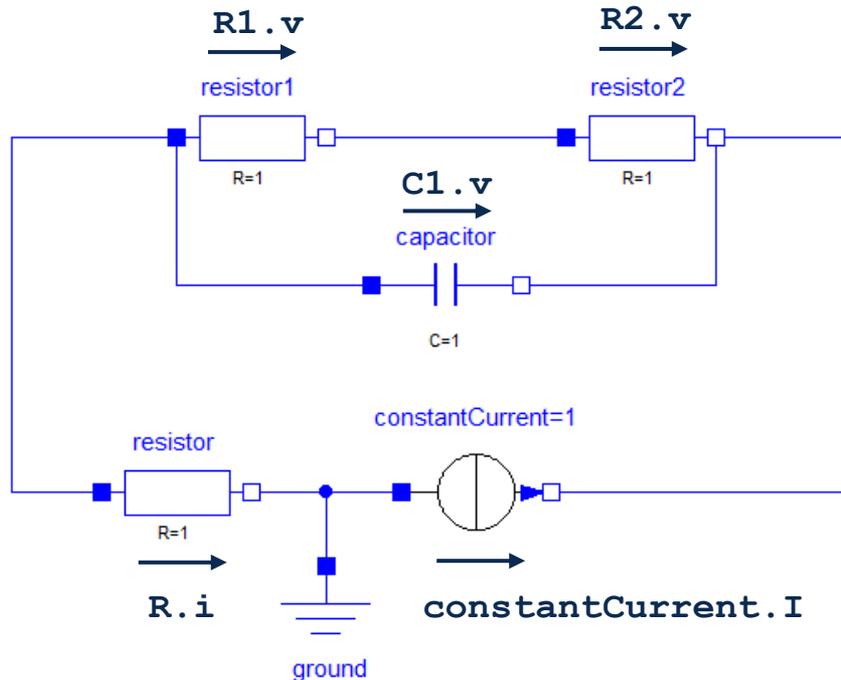


$$\begin{aligned}
 R1.v &= R.v - R1.n.v \\
 C1.v &= R.v + \text{constantCurrent.v} \\
 R2.v &= R1.n.v + \text{constantCurrent.v}
 \end{aligned}$$

$$0.0 = C1.v + (-R2.v) - R1.v$$

$$\begin{aligned}
 R.i + R1.i + C1.i &= 0.0 \\
 (-C1.i) - \text{constantCurrent.I} - R1.i &= 0.0
 \end{aligned}$$

$$0.0 = \text{constantCurrent.I} - R.i$$



Kirchhoff's current law

$$0.0 = constantCurrent.I - R.i$$

Kirchhoff's voltage law

$$0.0 = C1.v + (-R2.v) - R1.v$$

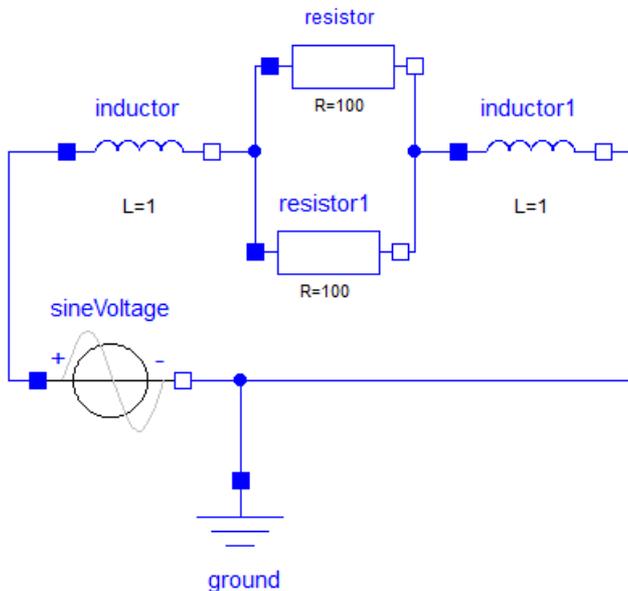
connect equations \longrightarrow node and mesh equations
(similar to fluid domain)

What is the effect of resolving loops?

For the presented model:

	no resolveLoops	with resolveLoops
equation system	{8x8} system	{3x3} system
speed up		1.14

→ reduce size of equation systems



no
resolveLoops



```

Error: When solving linear system
1 : resistor.i + resistor1.i - inductor.i = 0.0
2 : inductor1.i + (-resistor1.i) - resistor.i = 0.0
.
.
.
U(2,2) = 0.0, which means system is singular for
variable resistor1.i.
    
```

2 (equal) states

with
resolveLoops



resolved equations:

```

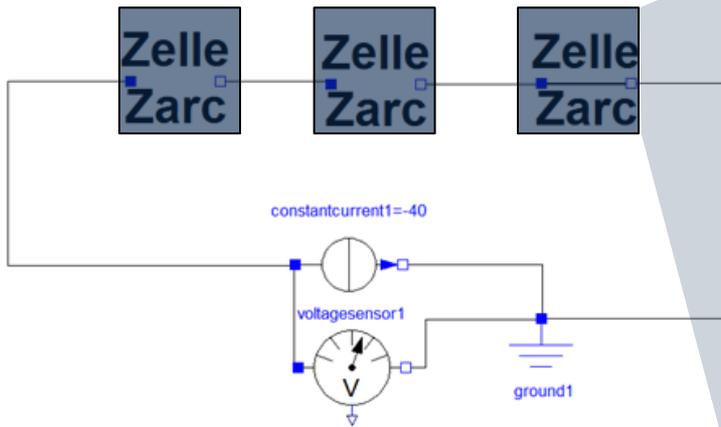
0.0 = -ground.p.i
0.0 = inductor.i - inductor1.i
0.0 = resistor1.v - resistor.v
    
```

1 state

simulation succeeds

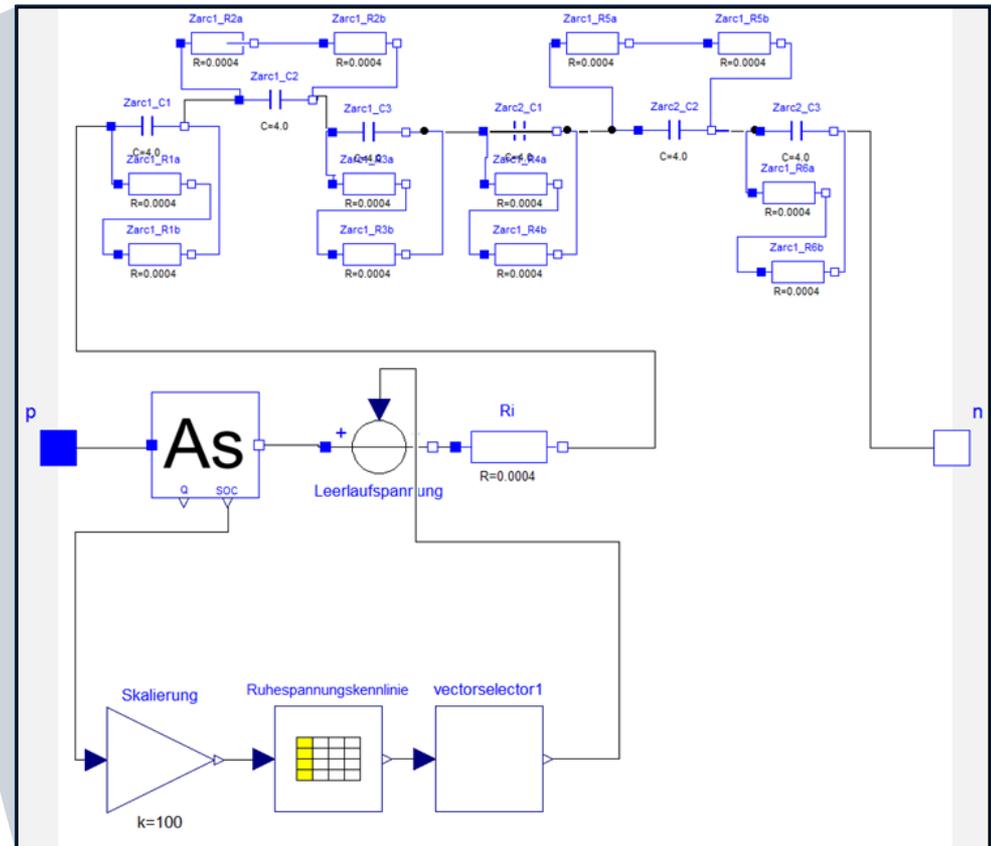
Dymola User Manual Volume 2
p. 361

→ prevent singular systems

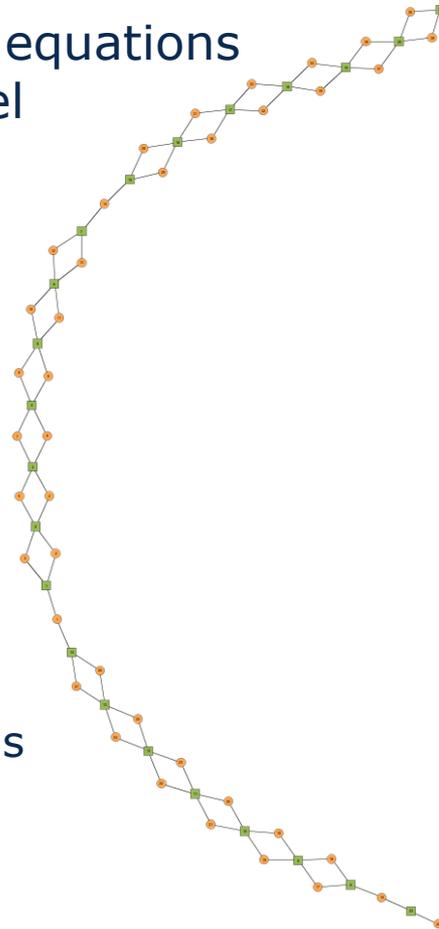


simplified battery model
for a hybrid car
(3 cells)

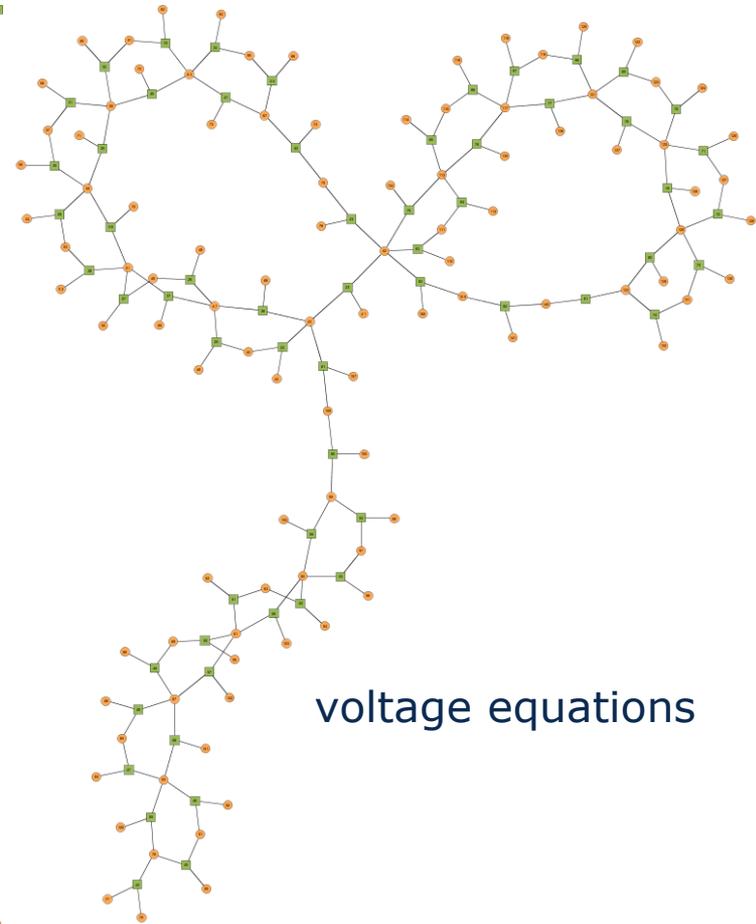
→ real model has 30 cells



bipartite graph
of the “resolvable” equations
of the battery model

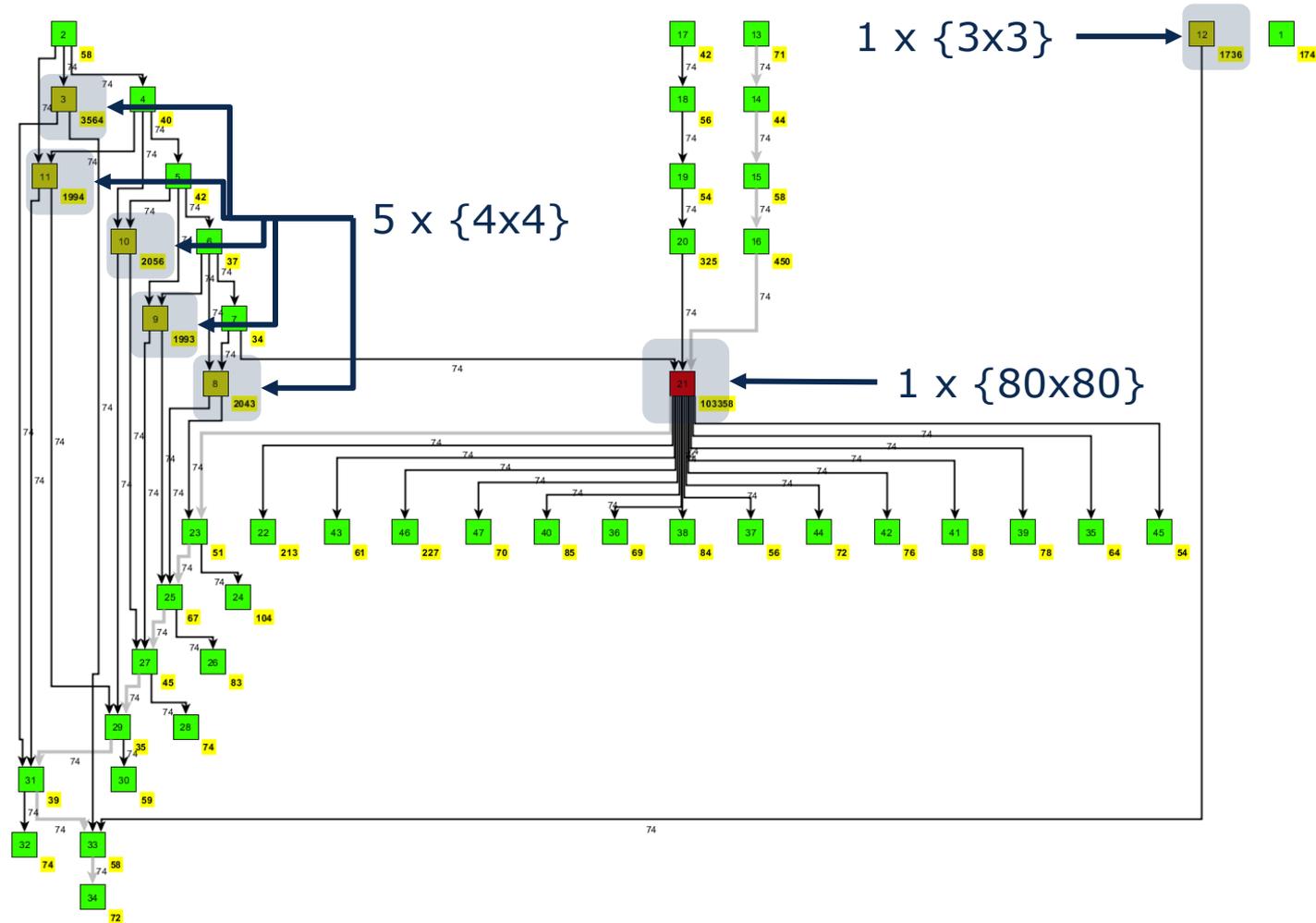


current equations



voltage equations

task graph
without
resolveLoops



18 x {3x3} →

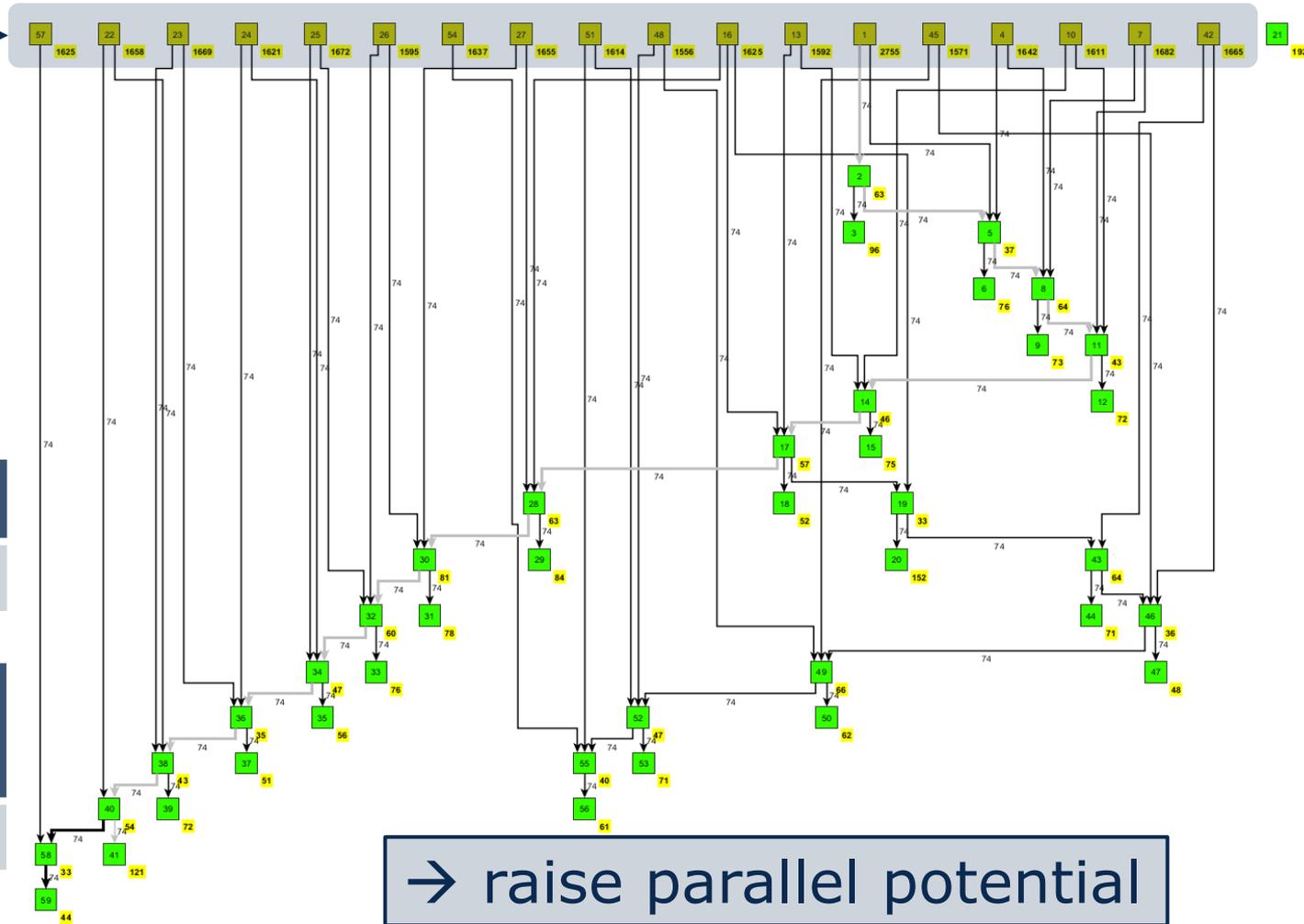
task graph
with
resolveLoops

serial speedUp

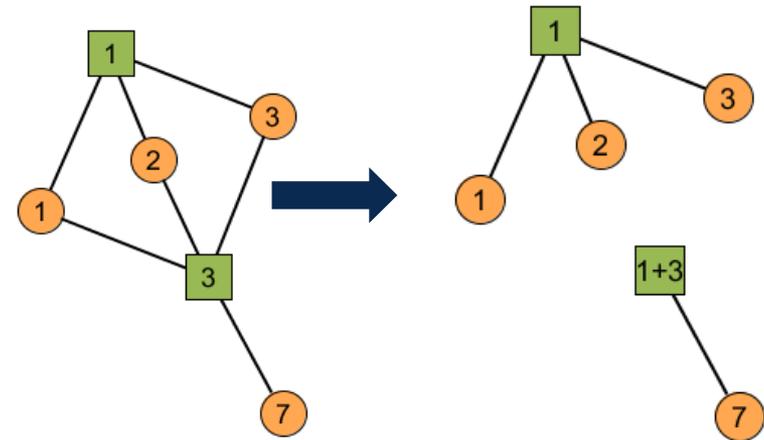
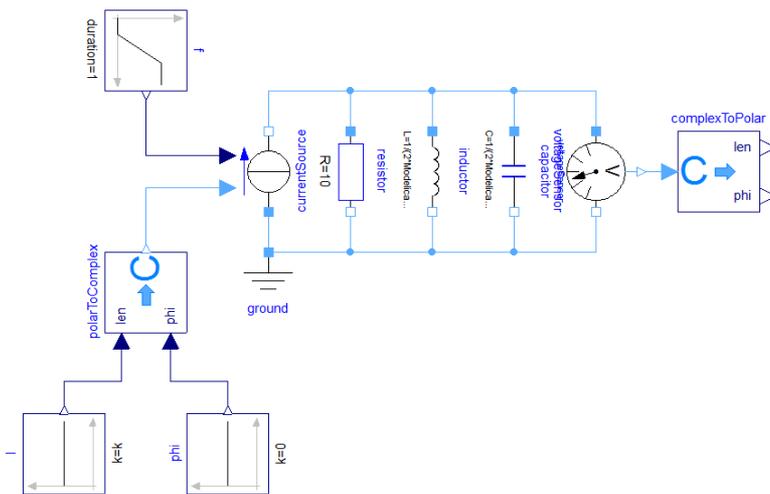
1.98

**serial speedUp
(30 cells)**

36.06



Electrical.QuasiStationary.SinglePhase.Examples.ParallelResonance



	no resolveLoops	with resolveLoops
strong Components	8 single equations	6 single equations

→ reduce number of SCCs

Summary

- Resolving algebraic loops can lead to:
 - splitting up systems of equations
 - prevent singular systems
 - reduce number of ODE-equations
 - raise parallel potential
- Serial and parallel speed up

Outlook

- Clarify: When to solve a loop?
 - Before or after index reduction?
 - Search for singularities or all loops?
 - Which and how many equations shall be replaced?
 - ...
- Implementation for linear equations with constant coefficients
- Analyse more models from different domains



»Wissen schafft Brücken.«

Volker Waurich
Dresden University of Technology
volker.waurich@tu-dresden.de
<http://tu-dresden.de/bft>